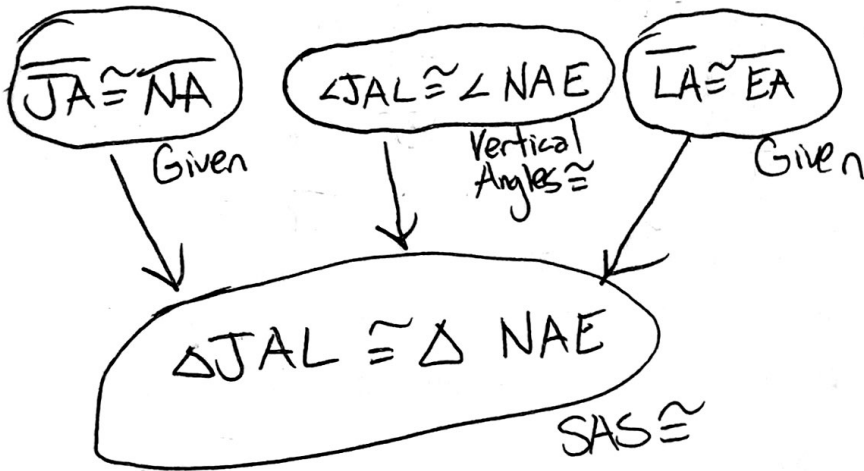
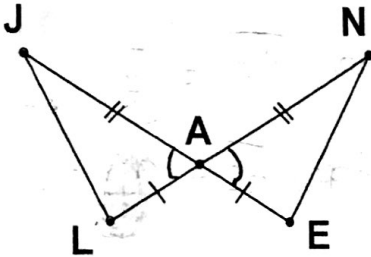


G5: Triangle and Quadrilateral Application and Proof

C-Level:

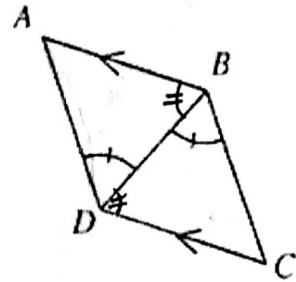
Use a flowchart or two-column proof to prove the triangles in the figure are congruent.



Statements	Reasons
① $\overline{JA} \cong \overline{NA}$	① Given
② $\angle JAL \cong \angle NAE$	② Vertical Angles
③ $\overline{LA} \cong \overline{EA}$	③ Given
④ $\triangle JAL \cong \triangle NAE$	④ SAS

B - Level:

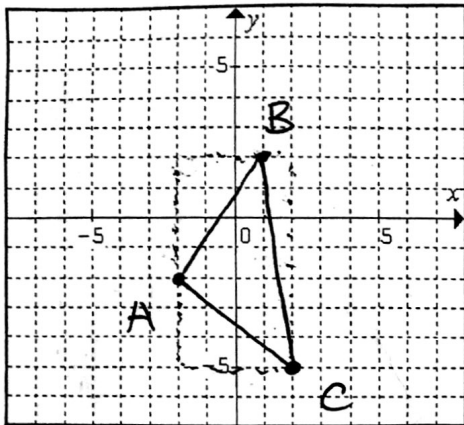
Use a flowchart or two-column proof to prove $\overline{AD} \cong \overline{BC}$



Statements	Reasons
① $\overline{AB} \parallel \overline{DC}$	① Given
② $\angle ABD \cong \angle CDB$	② Alternate Interior Angles
③ $\overline{BD} \cong \overline{DB}$	③ Reflexive Property
④ $\angle ADB \cong \angle CBD$	④ Given
⑤ $\triangle ADB \cong \triangle CBD$	⑤ ASA
⑥ $\overline{AD} \cong \overline{BC}$	⑥ CPCTC

G6: Coordinate Geometry

C - Level: Plot and connect points A (-2, -2), B (1, 2) and C (2, -5). What kind of triangle is this? Mathematically justify. What is the perimeter?



$$\begin{aligned} \overline{AB} &= \sqrt{4^2 + 3^2} \\ &= \sqrt{16+9} \\ &= \sqrt{25} = 5 \end{aligned}$$

$$\begin{aligned} \overline{BC} &= \sqrt{1^2 + 7^2} \\ &= \sqrt{1+49} \\ &= \sqrt{50} \\ &\approx 7.07 \end{aligned}$$

$$\begin{aligned} \overline{AC} &= \sqrt{3^2 + 4^2} \\ &= \sqrt{9+16} \\ &= \sqrt{25} \\ &= 5 \end{aligned}$$

$$\text{slope } \overline{AB} = \frac{4}{3}$$

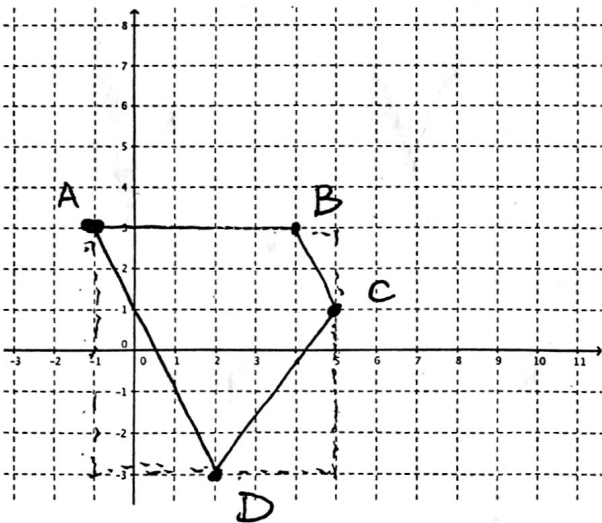
$$\text{slope } \overline{AC} = -\frac{3}{4}$$

negative reciprocals
 $\angle A = 90^\circ$

$\triangle ABC$ is a right
 Isosceles

$$P = 5 + 7.07 + 5 = 17.07 \text{ units}$$

B - Level: Plot and connect the points of ABCD if A(-1, 3), B(4, 3), C(5, 1), D(2, -3). Determine the most accurate name for the shape and justify your answer with calculations.



$$\overline{AB} = 5 \text{ units}$$

$$\begin{aligned} \overline{BC} &= \sqrt{1^2 + 2^2} \\ &= \sqrt{1+4} = \sqrt{5} \\ &\approx 2.24 \text{ units} \end{aligned}$$

$$\begin{aligned} \overline{DC} &= \sqrt{3^2 + 4^2} \\ &= \sqrt{9+16} \\ &= \sqrt{25} = 5 \text{ units} \end{aligned}$$

$$\begin{aligned} \overline{AD} &= \sqrt{3^2 + 6^2} \\ &= \sqrt{9+36} \\ &= \sqrt{45} \approx 6.71 \text{ units} \end{aligned}$$

$$\begin{aligned} \text{Perimeter} &= 5 + 2.24 + 5 + 6.71 \\ &= 18.95 \text{ units} \end{aligned}$$

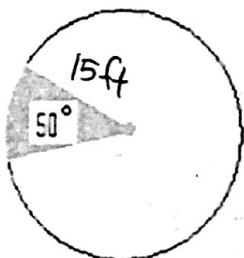
$$\text{slope } \overline{BC} = -\frac{2}{1}$$

$$\text{slope } \overline{AD} = -\frac{2}{1}$$

isosceles trapezoid

Level:

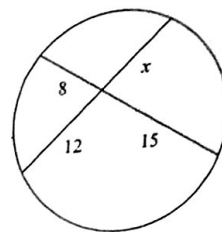
a. Find the area of the shaded region and the arc length if the radius is 15 ft.



Area of Sector
 $= \left(\frac{50}{360}\right) \pi 15^2$
 $\approx 98.17 \text{ ft}^2$

Arc Length
 $= \left(\frac{50}{360}\right) 2\pi(15)$
 $\approx 13.09 \text{ ft}$

b. Solve for x.



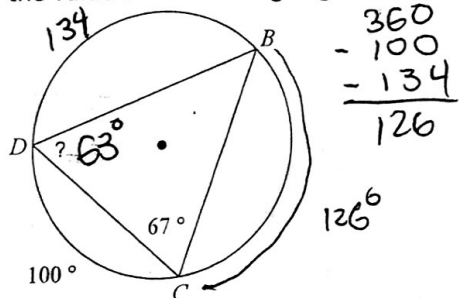
$$12x = 8 \cdot 15$$

$$\frac{12x}{12} = \frac{120}{12}$$

$$x = 10$$

B - Level:

a. Find the value of the missing angle.



$$\begin{array}{r} 360 \\ - 100 \\ - 134 \\ \hline 126 \end{array}$$

b. Identify the center and radius of the following circle:

$$x^2 + (y-5)^2 = 20$$

center = (0, 5)

radius = $\sqrt{20} \approx 4.47$

G8: Solids

C - Level: Find the surface Area and Volume of the following solids

a. 12 m



$$SA = (\pi \cdot 5 \cdot 13) + (\pi \cdot 5^2)$$

$$= 204.20 + 78.5398$$

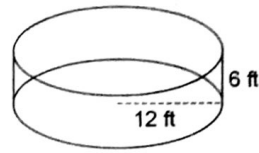
$$SA = 272.74 \text{ m}^2$$

$$V = \left(\frac{1}{3}\right) \cdot \pi \cdot 5^2 \cdot 12$$

$$= \left(\frac{1}{3}\right) \cdot 300\pi$$

$$V = 100\pi \approx 314.16 \text{ m}^3$$

b.



$$SA = 2\pi(12)(6) + 2\pi(12)^2$$

$$= 452.389 + 904.778$$

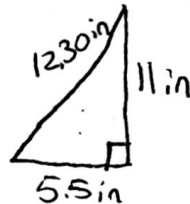
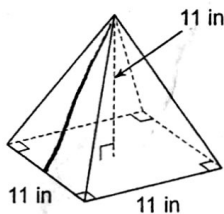
$$SA = 1357.17 \text{ ft}^2$$

$$V = \pi \cdot 12^2 \cdot 6$$

$$V \approx 2714.34 \text{ ft}^3$$

B - Level: Complete both parts.

a. Find the surface area of the pyramid

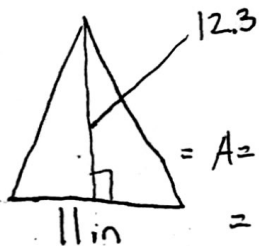


$$5.5^2 + 11^2 = c^2$$

$$30.25 + 121 = c^2$$

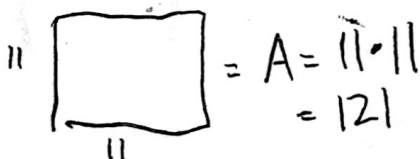
$$151.25 = c^2$$

$$c = 12.30$$



$$A = \frac{1}{2} \cdot 11 \cdot 12.3$$

$$= 67.65$$



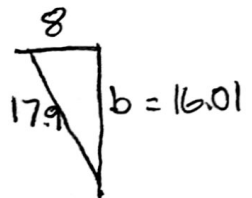
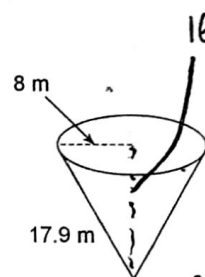
$$A = 11 \cdot 11$$

$$= 121$$

$$S.A. = 4(67.65) + 121$$

$$SA = 391.6 \text{ in}^2$$

b. Find the volume of the cone



$$8^2 + b^2 = 17.9^2$$

$$64 + b^2 = 320.41$$

$$-64 \quad -64$$

$$b^2 = 256.41$$

$$b = 16.01$$

$$V = \left(\frac{1}{3}\right) \cdot \pi \cdot 8^2 \cdot 16.01$$

$$= \left(\frac{1}{3}\right) \pi \cdot 1024.64$$

$$V \approx 1073 \text{ m}^3$$